

COUNTING

- Triangle *
- रेखा (Line) *
- Square *
- Rectangle *
- Quadrilateral *
- Pentagon *
- Polygon *
- Circle *
- Cube *

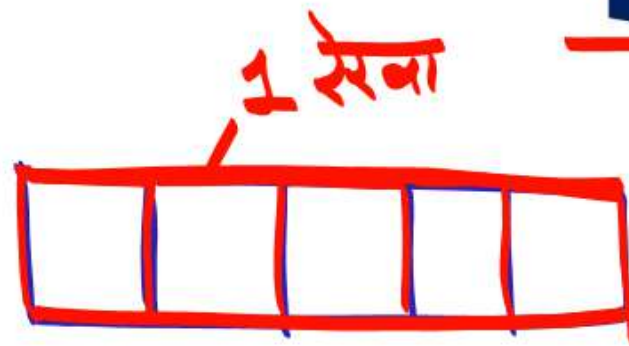
OF

आकृतियों की गणना

Approach → Construction
+
Combination ✓

FIGURE

Counting of Straight Lines



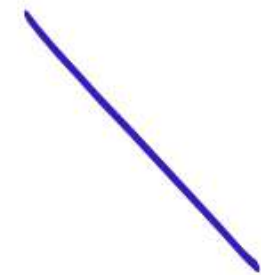
$$2 + 6 + 0 = 8$$

रेखाओं की गणना

— सॉलिड

उद्बिध

त्रिभुज



Count as follows

क्षैतिज
A. Horizontal line A————B

उर्ध्वाधर
B. Vertical line

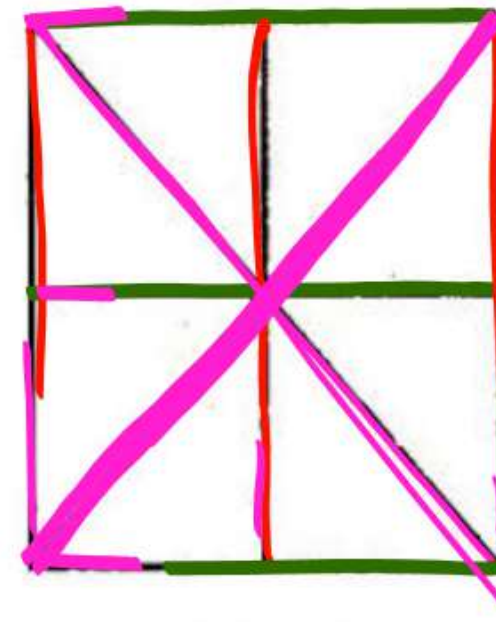
A
B

तिर्धक
C. Slant line

A A
B B

Ex. Number of lines in the given figure?

$$\begin{array}{ccccc}
 H & & V & & T \\
 3 & + & 3 & + & 2 = 8
 \end{array}$$



(a) 14

✓ (b) 8

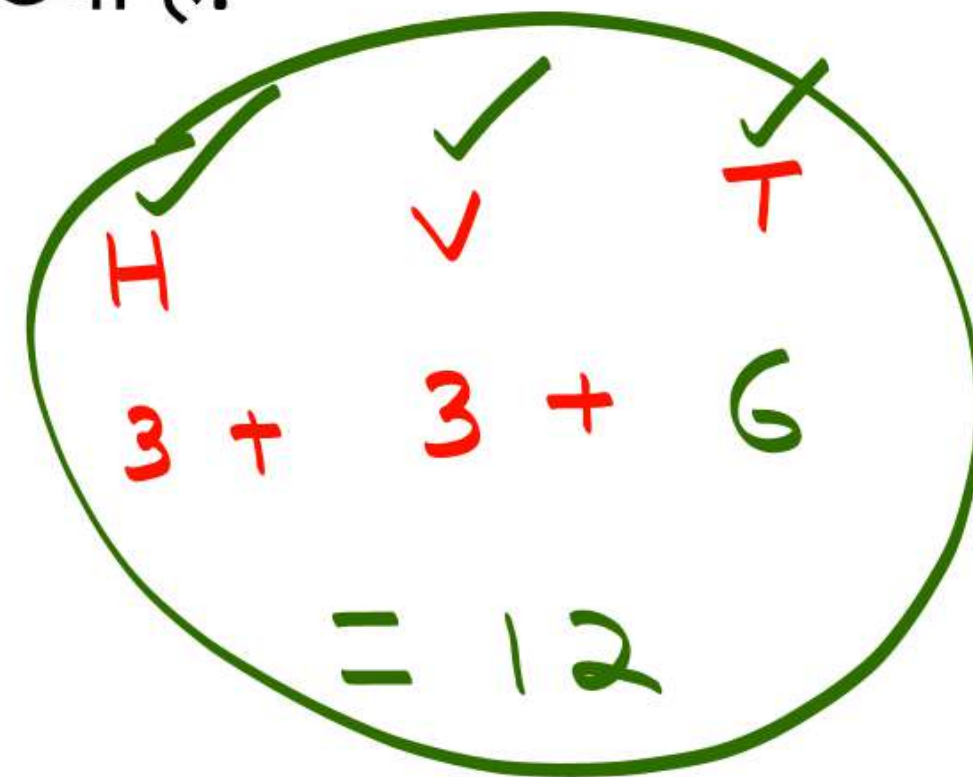
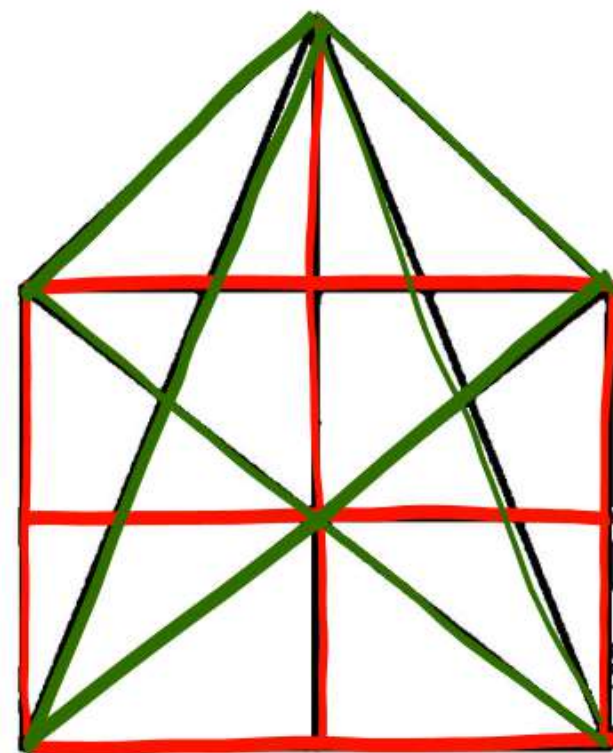
(c) 4

(d) 9

QUESTION 1

The number of straight lines in the figure is:

आकृति में सीधी रेखाओं की संख्या है:



(a) 10

✓ (c) 12

(b) 11

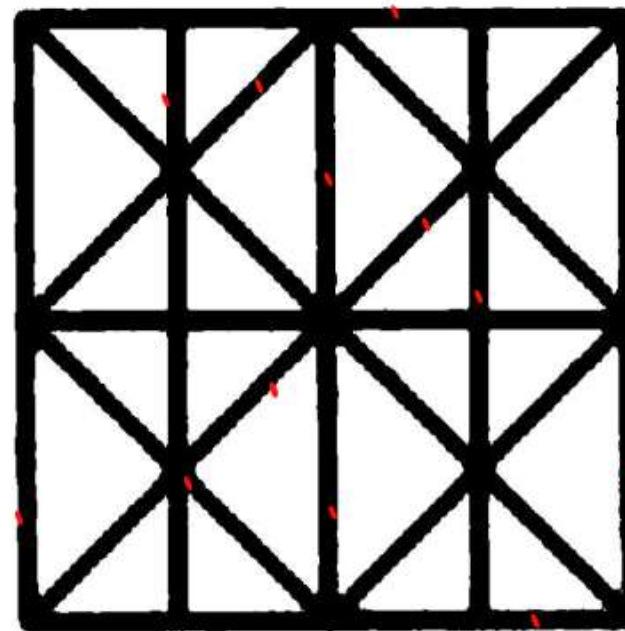
(d) 13

QUESTION 2

Find the minimum number of straight lines required to make the given figure.

दी गई आकृति को बनाने के लिए आवश्यक न्यूनतम सीधी रेखाओं की संख्या ज्ञात कीजिए।

figure counting X



$$\begin{array}{c} H \\ 3 \end{array} + \begin{array}{c} V \\ 5 \end{array} + \begin{array}{c} T \\ 6 \end{array} = 14$$

(a) 11

(c) 16

☒ (b) 14

(d) 17

Counting of squares

वर्ग की गणना

SQUARE (वर्ग)

Standard Pattern (मानक पैटर्न)

	1^2	2^2	3^2	4^2	5^2

शर्त

पंक्ति = स्तम्भ

Rows = Columns
5 = 5

Total वर्ग
कुल Square =

$$1^2 + 2^2 + 3^2 + 4^2 + 5^2$$

$$1 + 4 + 9 + 16 + 25$$

$$\Rightarrow 55 \checkmark$$

$$* 1^2 + 2^2 + \dots + N^2$$

$$\text{Sum} = \frac{N(N+1)(2N+1)}{6}$$

$$\frac{5(5+1)(5 \times 2 + 1)}{6} = \frac{5 \times 6 \times 11}{6} = 55 \checkmark$$

शर्त: $\rightarrow$ जब मैट्रिक्स के रूप में आकृति हो।
MATRIX

Row = 3

Column = 2

Method

$R \times C$ पंक्ति $\times$ स्तम्भ

$$\begin{array}{l} 3 \times 2 = 6 \\ 2 \times \textcircled{1} = 2 \\ 1 \times 0 = 0 \end{array}$$

8✓

1 ²	2 ²	3 ²

$$\begin{aligned} &\Rightarrow 1^2 + 2^2 + 3^2 \\ &\Rightarrow 1 + 4 + 9 = 14 \checkmark \end{aligned}$$

R = 3 C = 3

$$\begin{array}{l} 3 \times 3 = 9 \\ 2 \times 2 = 4 \\ \textcircled{1} \times 1 = 1 \end{array}$$

14✓

* How many Squares are there in a Chess Board?
 शतरंज बोर्ड में कितने वर्ग होते हैं

$N=8$

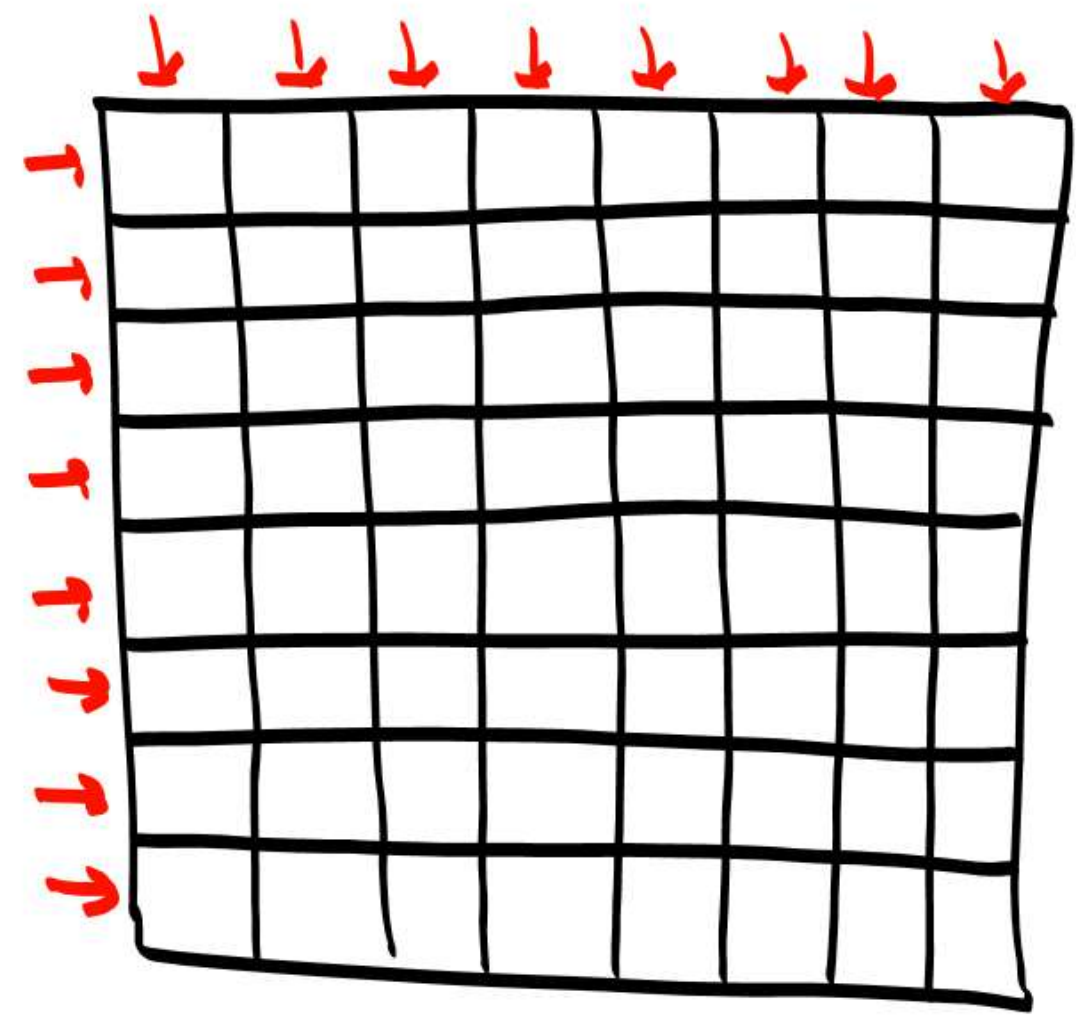
$$1^2 + 2^2 + 3^2 + 4^2 + 5^2 + 6^2 + 7^2 + 8^2 \Rightarrow$$

$$\text{Sum} = \frac{N(N+1)(2N+1)}{6}$$

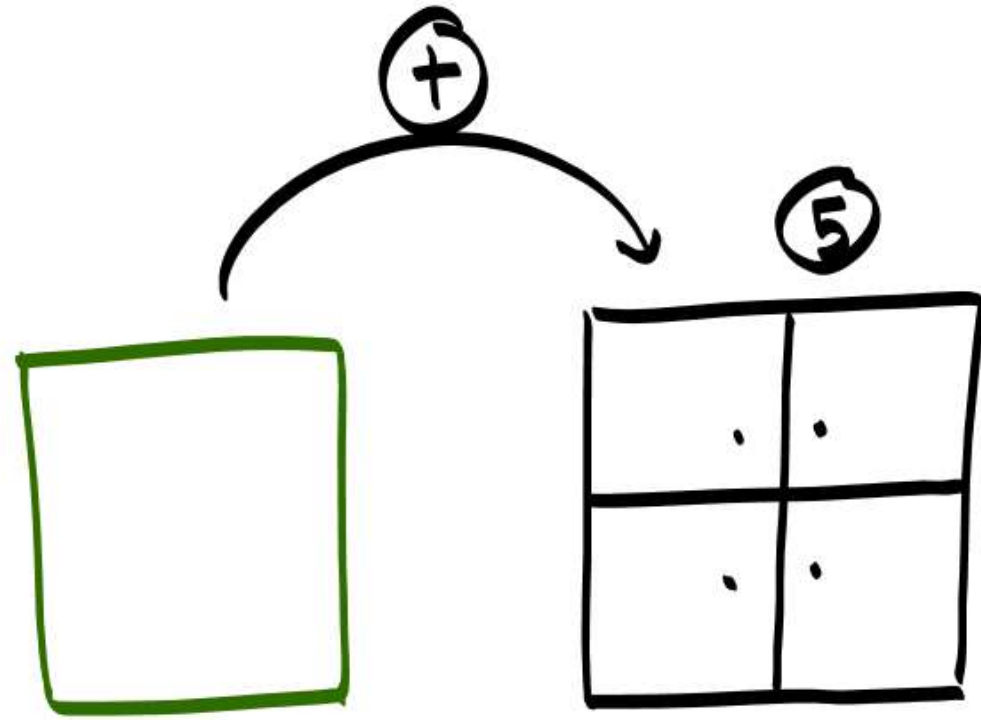
$$= \frac{8(8+1)(2 \times 8 + 1)}{6} \Rightarrow 204$$

Row $\rightarrow 8$

Column $\rightarrow 8$



$\left\{ \begin{array}{l} 8 \times 8 \\ 7 \times 7 \\ 6 \times 6 \\ 5 \times 5 \\ 4 \times 4 \\ 3 \times 3 \\ 2 \times 2 \\ 1 \times 1 \end{array} \right\} \Rightarrow 204$



वर्ग = 1

$$1 + 4 = 5$$

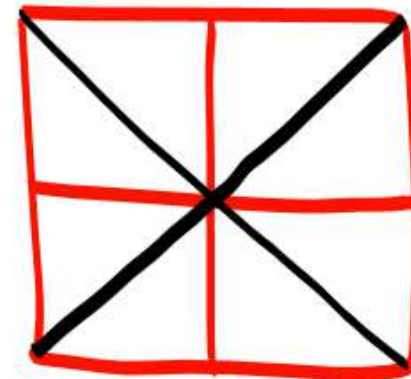
वर्ग (SQUARE)

चारो मुजाफे बराबर

चारो कोण = 90°

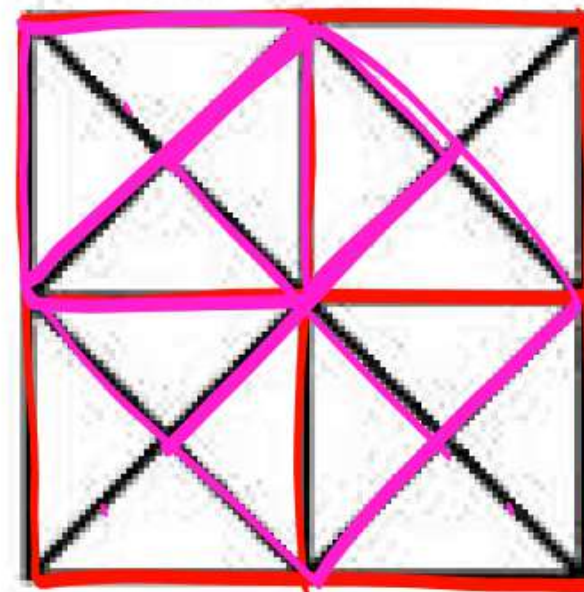
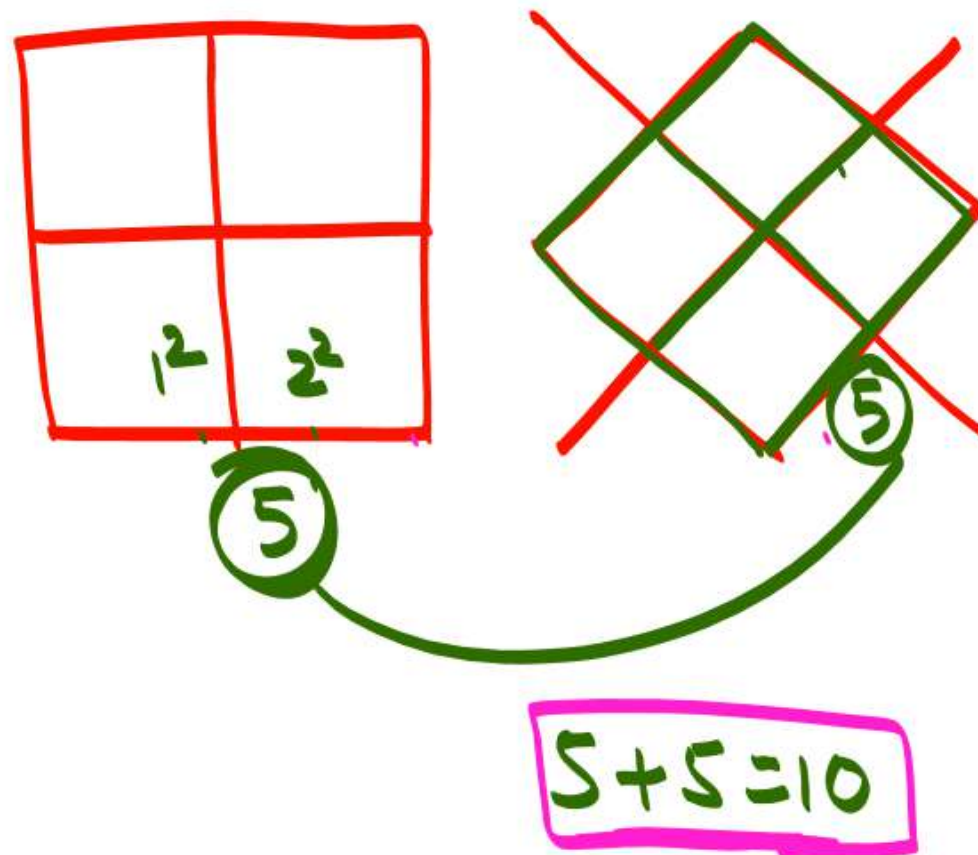
दोनों विकर्ण बराबर

Note $\Rightarrow$ All Squares are Rectangle
सभी वर्ग, आयत होते हैं



Find the total number of squares in the figure.

आकृति में कुल वर्गों की संख्या ज्ञात कीजिए।

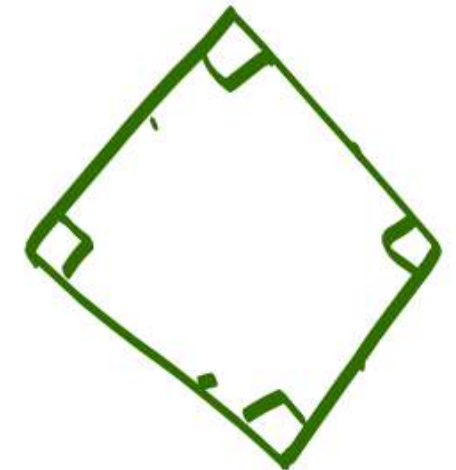


(a) 6

(c) 8

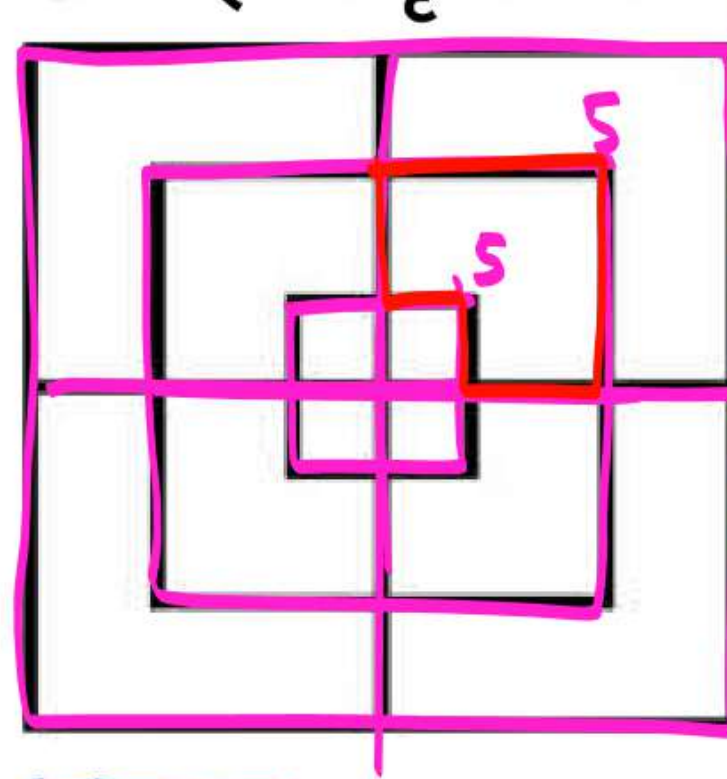
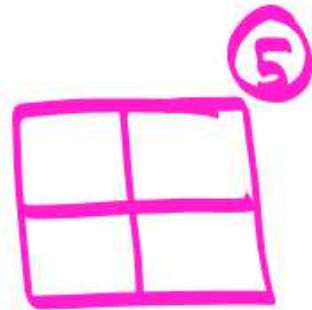
(b) 12

☒ (d) 10



How many maximum squares are there in the given figure?

दी गई आकृति में अधिकतम कितने वर्ग हैं?



~~(a) 12~~

(c) 18

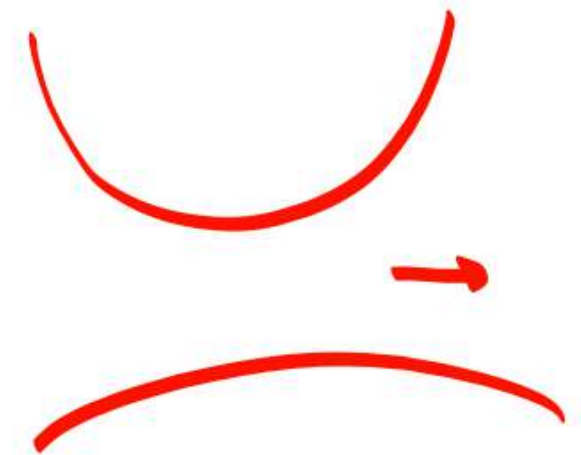
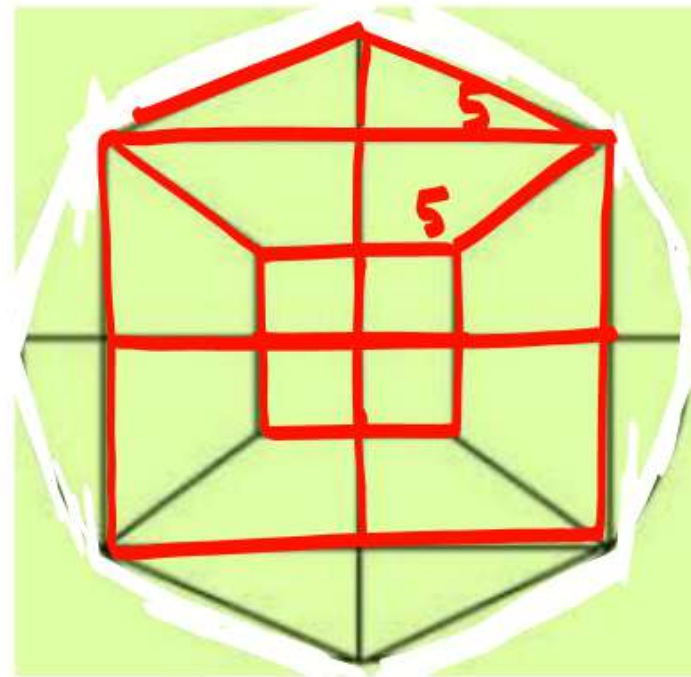
✓ (b) 15

~~(d) 8~~

How many squares are there in the given figure?

दी गई आकृति में कितने वर्ग हैं?

$$5 + 5 = 10 \checkmark$$



(a) 11

~~(b) 9~~

~~(c) 10~~

(d) 12

Q. No. :

4

How many squares are there in the given figure?

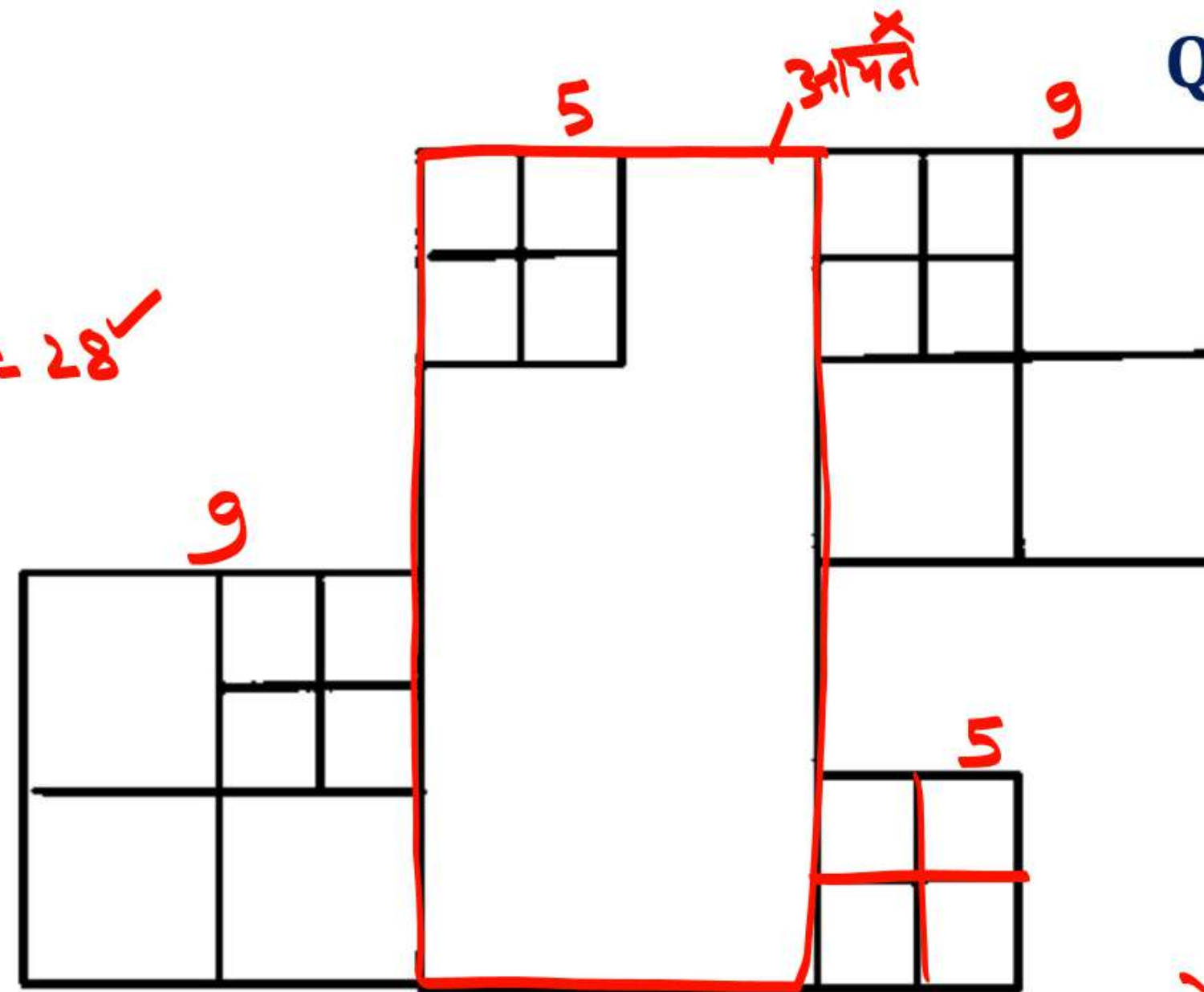
दी गई आकृति में कितने वर्ग हैं?

(a) 53

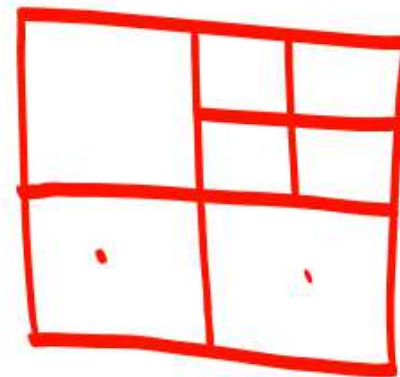
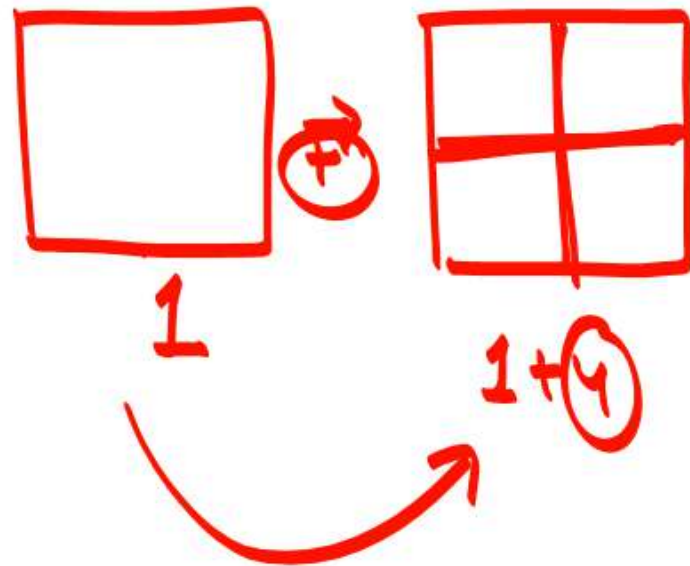
☒ (b) 28

(c) 27

(d) 54



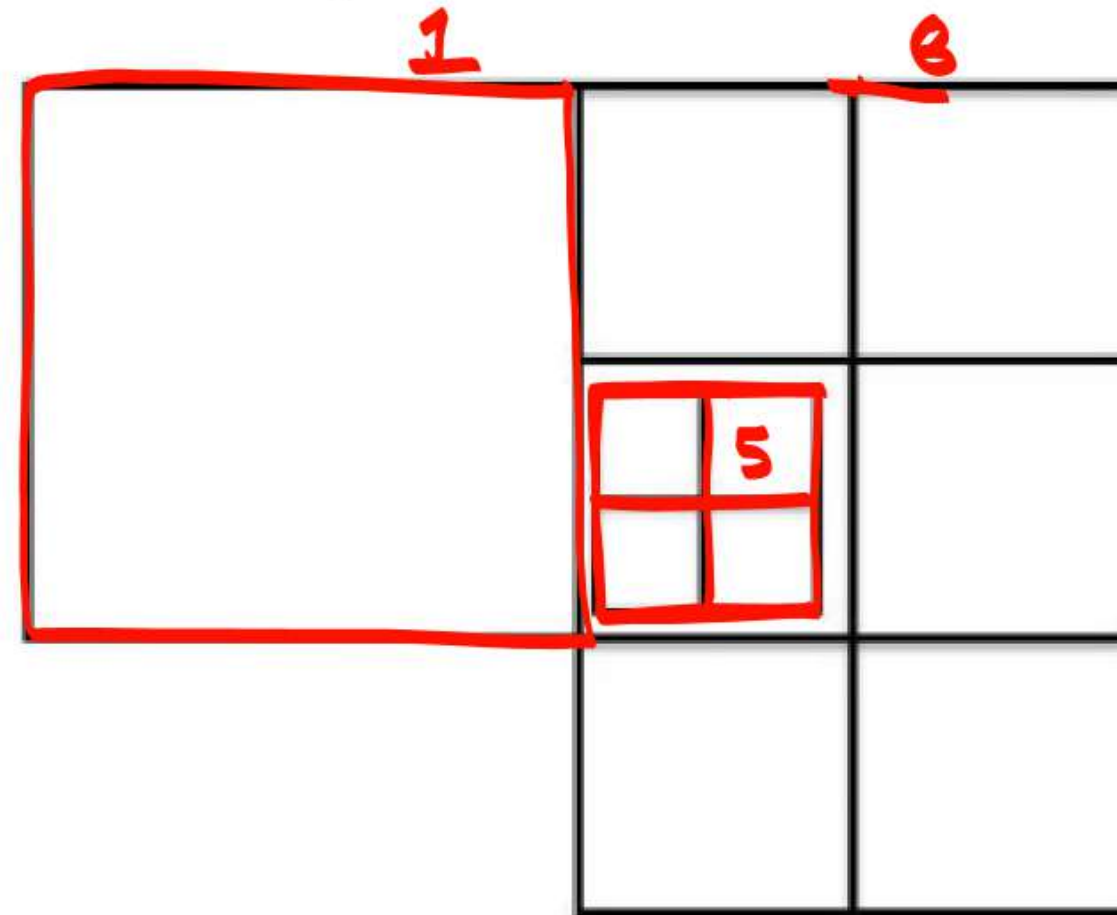
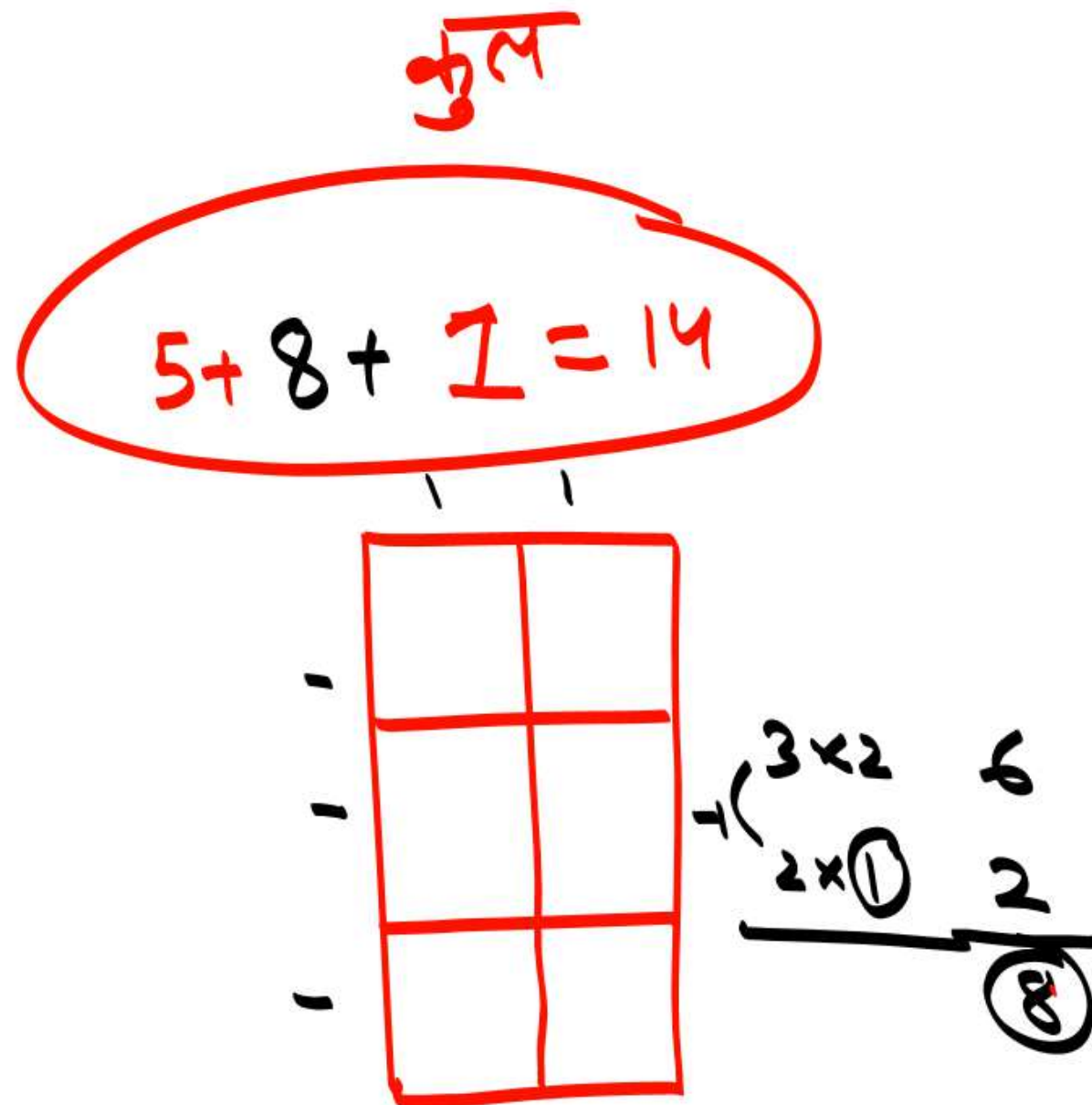
$$9 + 9 + 5 + 5 = 28$$



$$1 + 4 + 4 = 9$$

How many squares are there in the given figure?

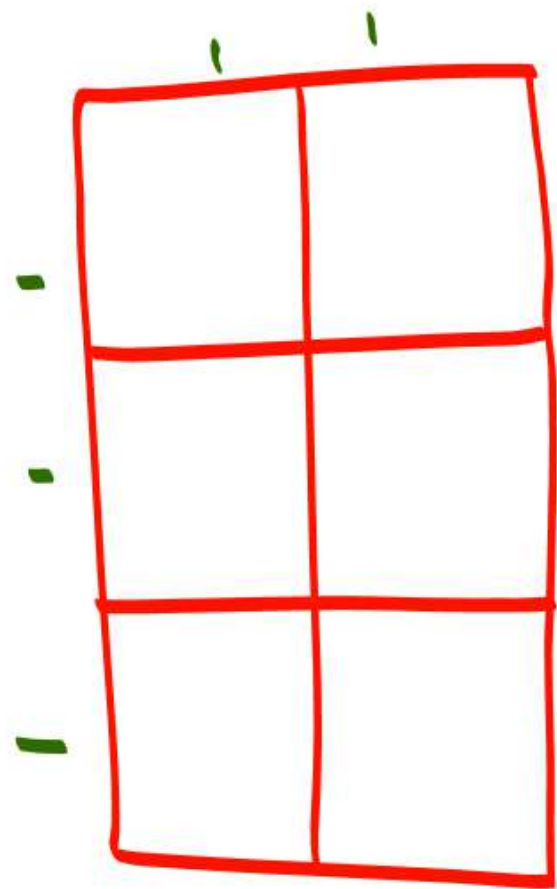
दी गई आकृति में कितने वर्ग हैं?



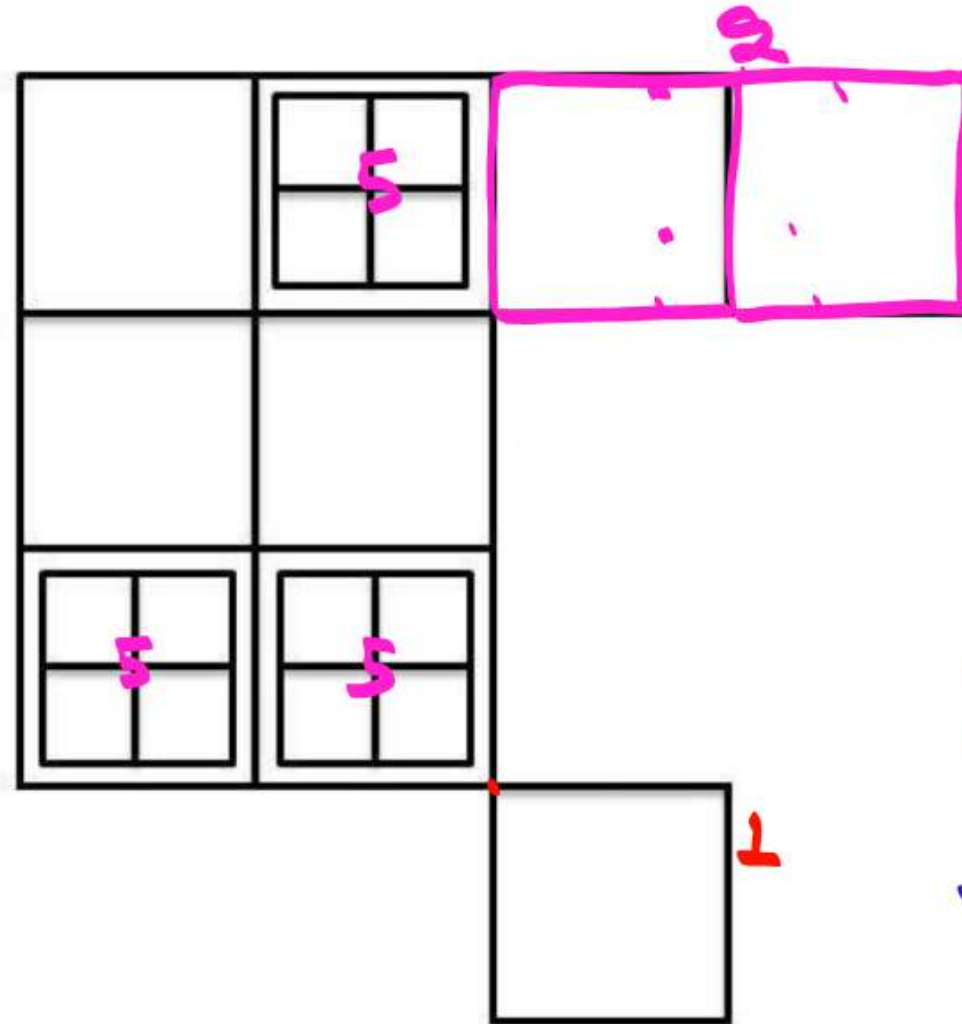
(A) 14
(C) 21

(B) 20
(D) 18

How many squares are there in the given figure?
दी गई आकृति में कितने वर्ग हैं?



$$\begin{array}{r} 3 \times 2 = 6 \\ 2 \times 1 = 2 \\ \hline 8 \end{array}$$



$$\begin{array}{l} \text{कुल} = \\ 1 + 5 + 5 + 5 + 8 + 2 \\ = 26 \end{array}$$

(A) 20

(B) 21

☒ (C) 26

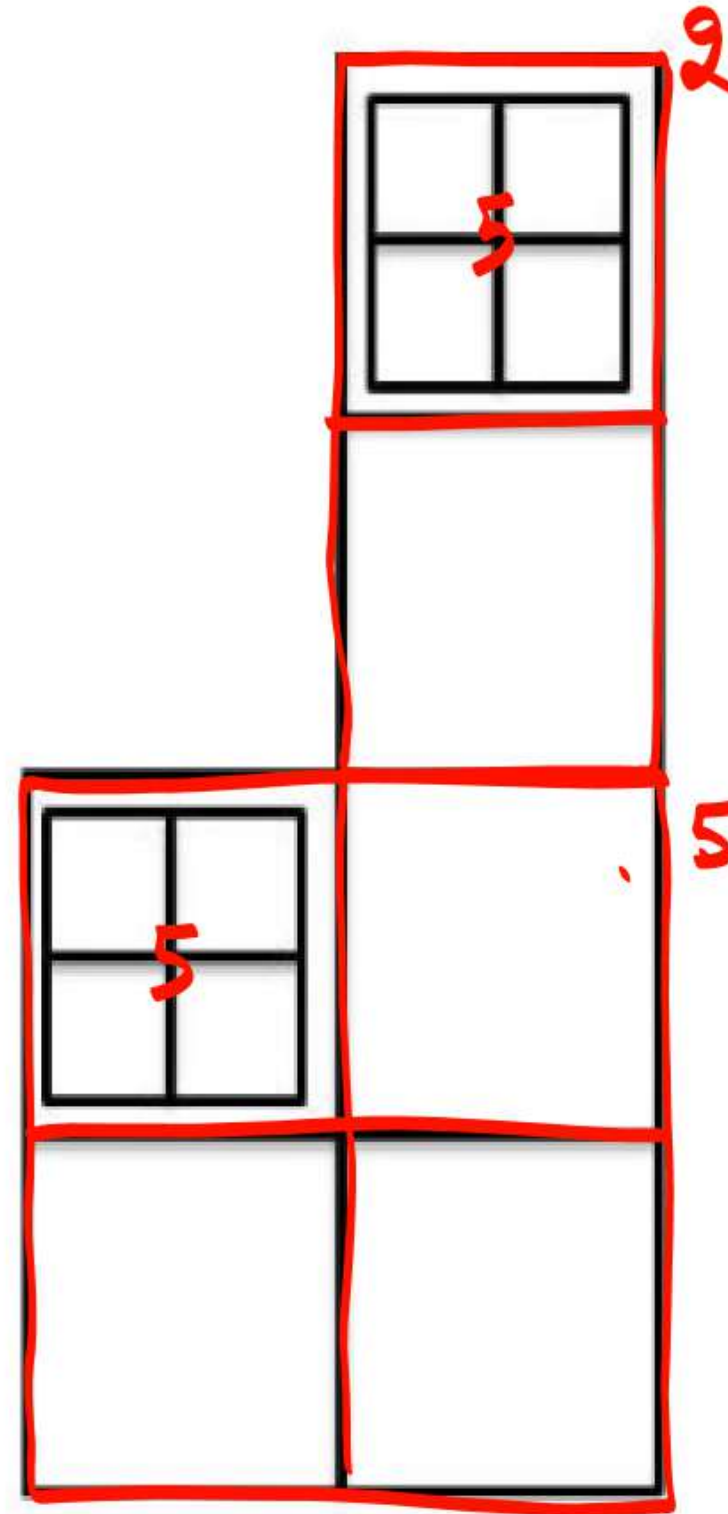
(D) 25

Q. No. :

7



$$5 + 5 + 5 + 2 \\ = 17 \checkmark$$



How many squares are there in the given figure?

दी गई आकृति में कितने वर्ग हैं?

- (A) 18
(C) 20

- ☒ (B) 17
(D) 21



Counting of Rectangles

અમને માનવે શી જુજાણે બરાબર
ચારો કોણ 90°
દોતો વિવર્ણ બરાબર

આયતો શી ગણના
Counting of Rectangles.

मैट्रिक्स (MATRIX)

1^3	2^3	3^3	4^3	5^3

R = 5 C = 5

शर्त (Condition) पांक्ति = स्तम्भ
Row = Column ✓

$$1^3 + 2^3 + 3^3 + 4^3 + 5^3 \Rightarrow$$
$$1 + 8 + 27 + 64 + 125 \Rightarrow 225 \checkmark$$

Formula

$$1^3 + 2^3 + 3^3 + \dots + N^3$$

$$\text{Sum} = \left[\frac{N(N+1)}{2} \right]^2$$

Sum $\rightarrow$ पूर्ण वर्ग
 $\rightarrow$ perfect square.

क्रमगत संख्याएँ

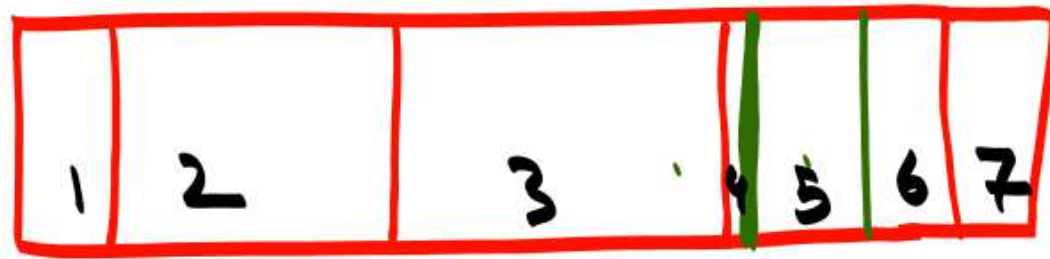
$$1 + 2 + 3 + \dots + N$$

$$\text{योग} = \frac{N(N+1)}{2}$$

$$\left[\frac{5(5+1)}{2} \right]^2$$

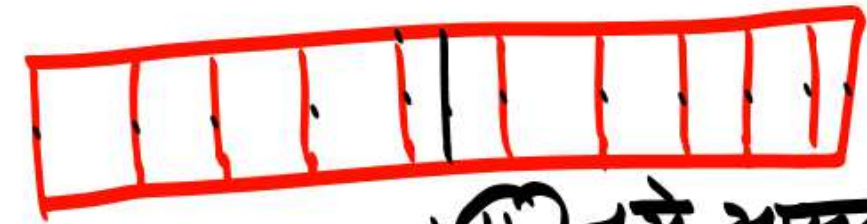
$$= \left[\frac{5 \times 6}{2} \right]^2 = 15^2 = 225 \checkmark$$

* Tricks/Methods/Concepts/Technique

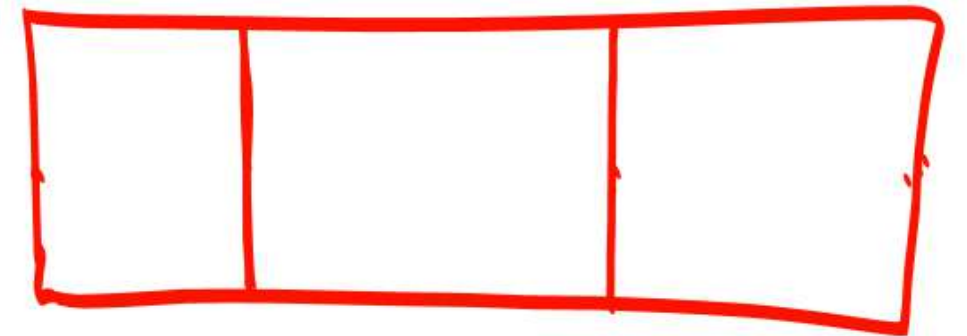


आयत
Rectangle

$$= 1 + 2 + 3 + 4 + 5 + 6 + 7$$
$$= \frac{N(N+1)}{2} = \frac{7 \times 8}{2} = 28 \checkmark$$



+ 11 नये आयत बनेंगे

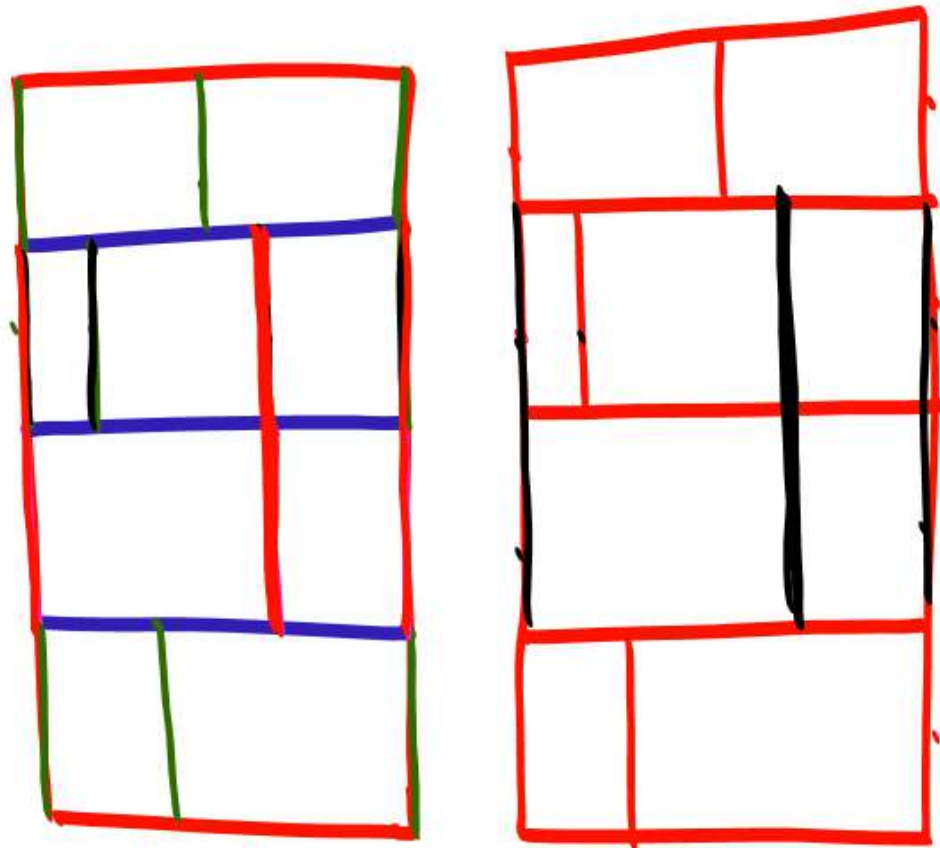


$$1 + 2 + 3$$

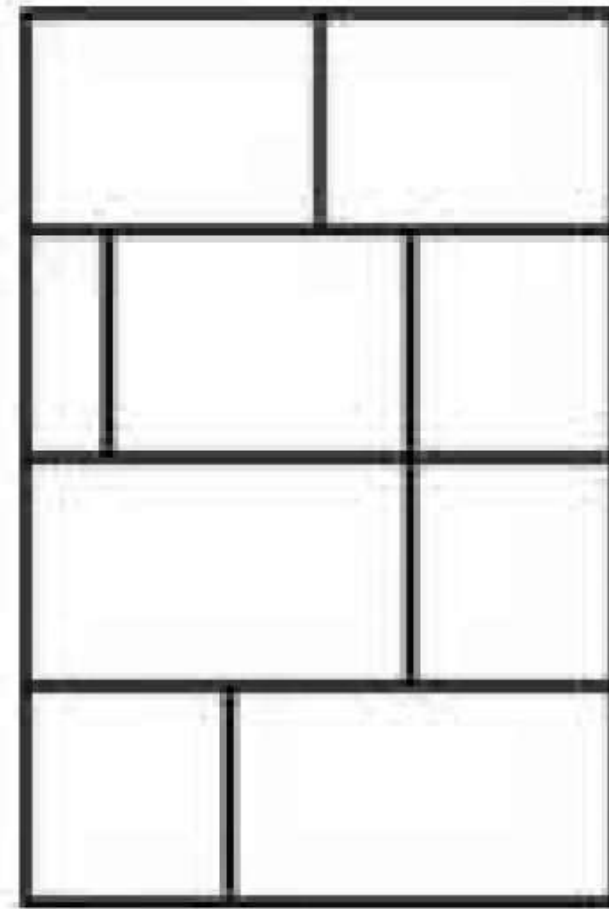
Construction

How Many quadrilaterals are there in the given figure ?

दी गई आकृति में कितने चतुर्भुज हैं?



$$\Rightarrow 1+2+3+4+2+2+2+3+2+2$$



(a) 24

(b) 25

(c) 22

(d) 23

आयत ✓

Q. No. :

9



How many quadrilaterals are there in the given figure ?

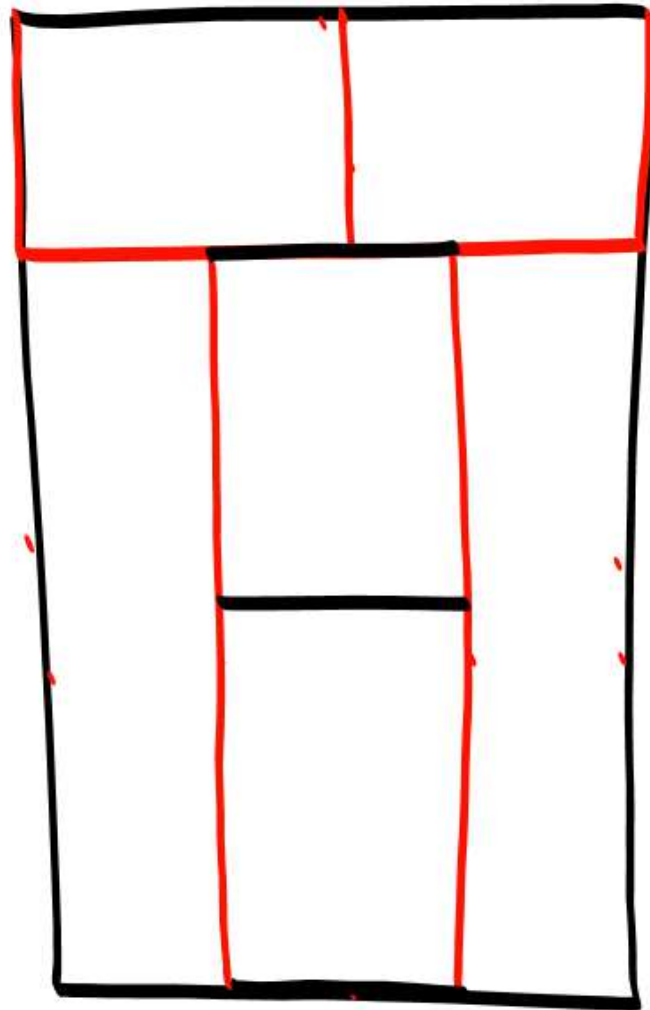
दी गई आकृति में कितने चतुर्भुज हैं?

(a) 14

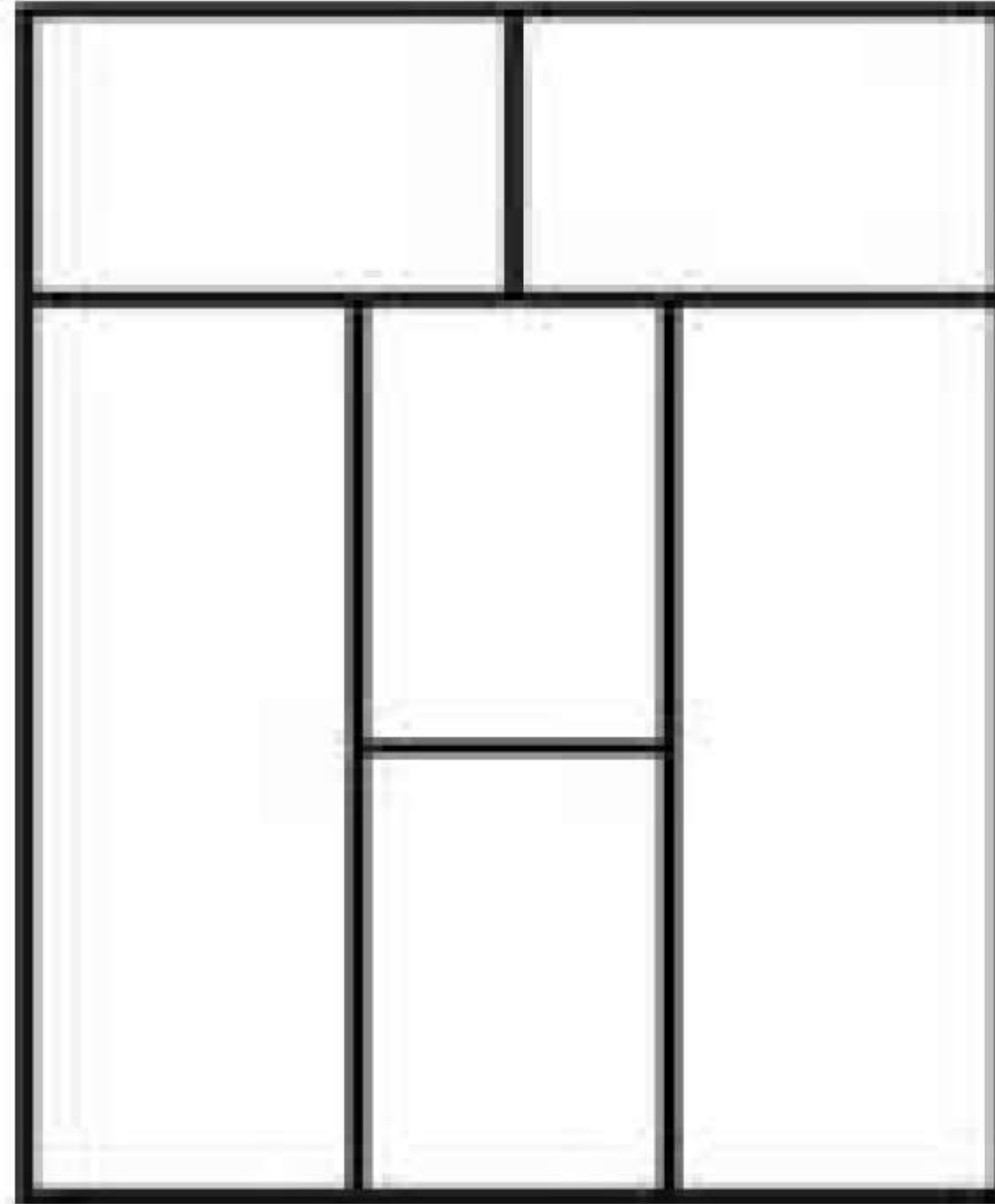
(b) 13

☒ (c) 12

(d) 11



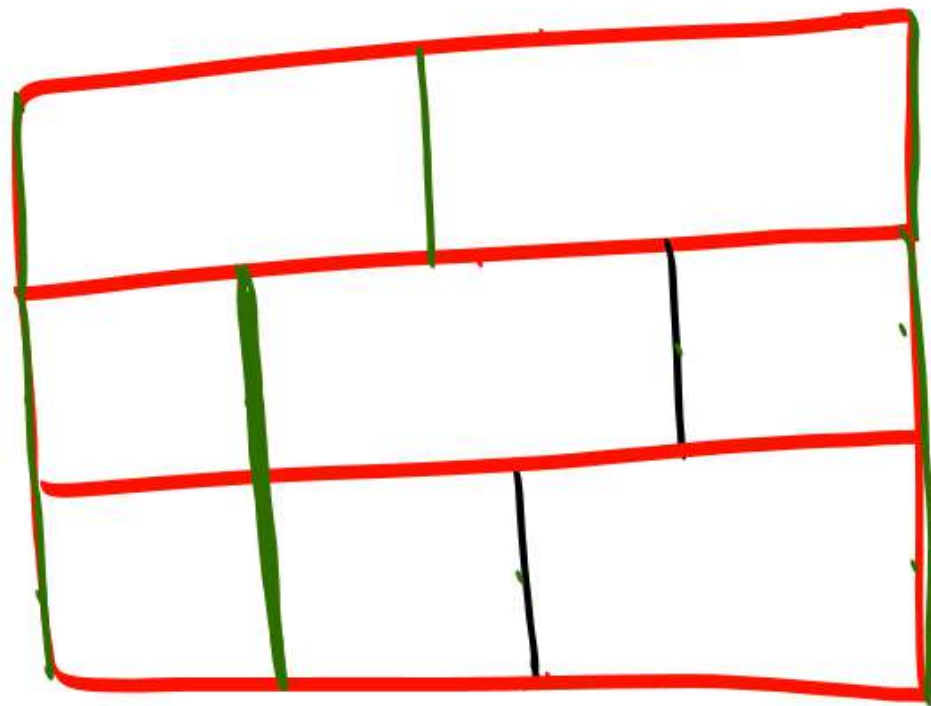
$1+2+2+2+3+2$ ✓



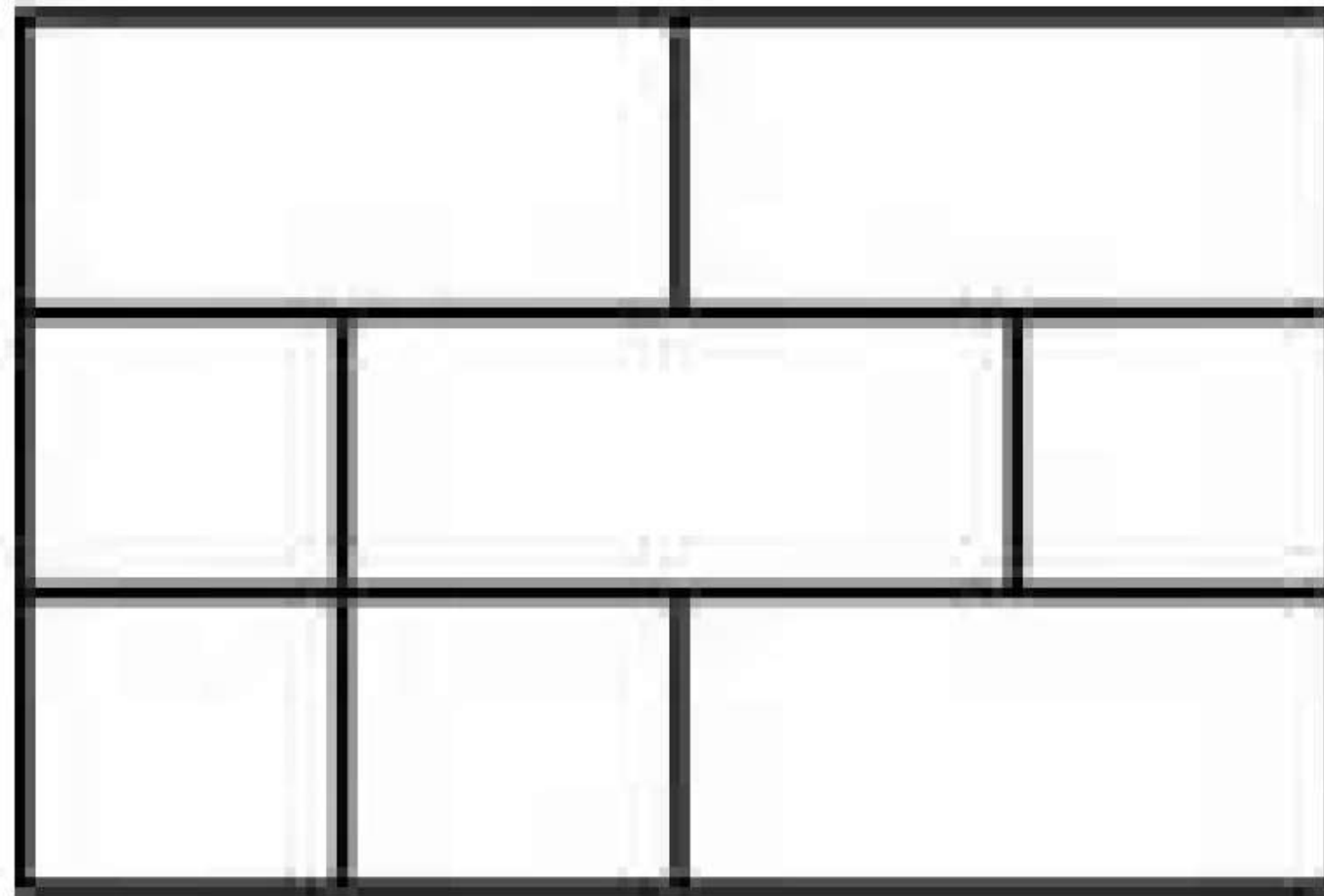
25.

How many quadrilaterals are there in the given figure ?

दी गई आकृति में कितने चतुर्भुज हैं?



$$\begin{aligned}
 &1 + 2 + 3 + 2 + 2 \\
 &+ 3 + 3 + 2 \Rightarrow 18 + 2 \\
 &= 20
 \end{aligned}$$



(a) 17

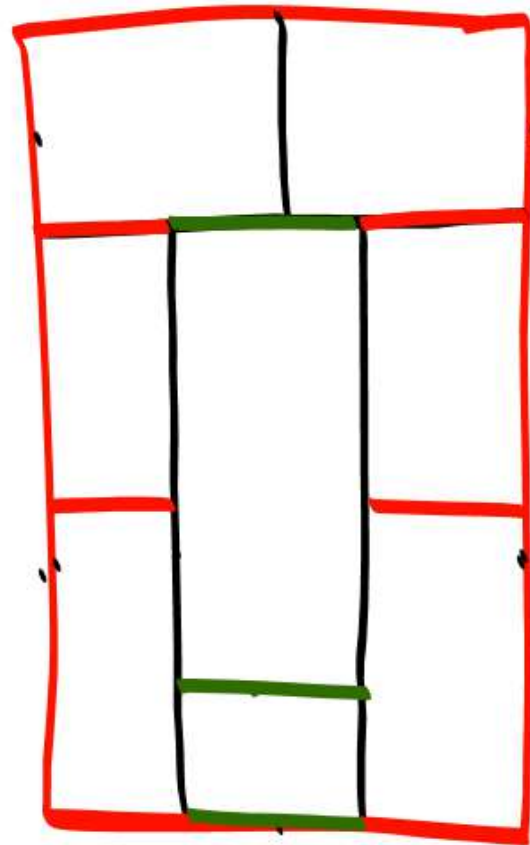
☒ (c) 20

(b) 19

(d) 18

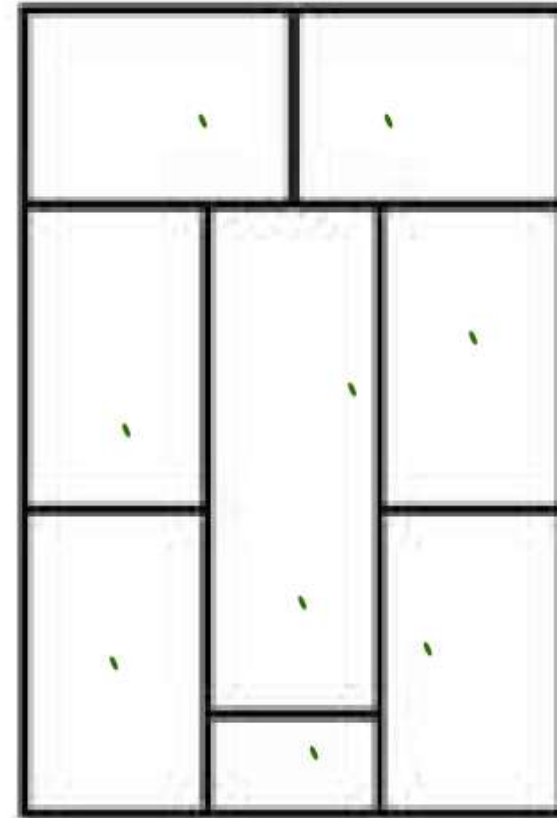
How many quadrilaterals are there in the given figure?

दी गई आकृति में कितने चतुर्भुज हैं?



$$1 + 2 + 2 + 2 + 3 + 2 + 2 + 2$$

$$\Rightarrow 16$$



(a) 15

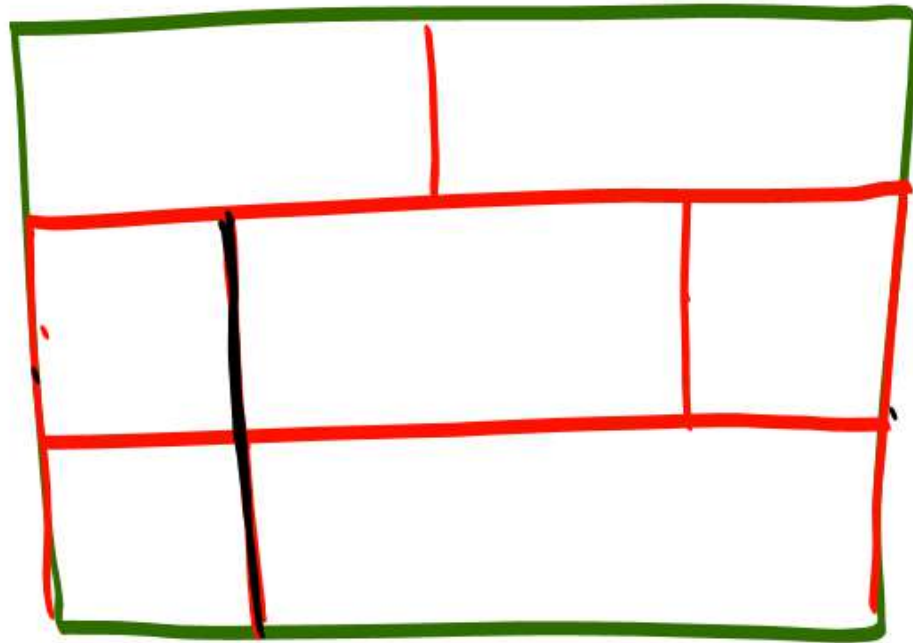
(c) 14

(b) 16

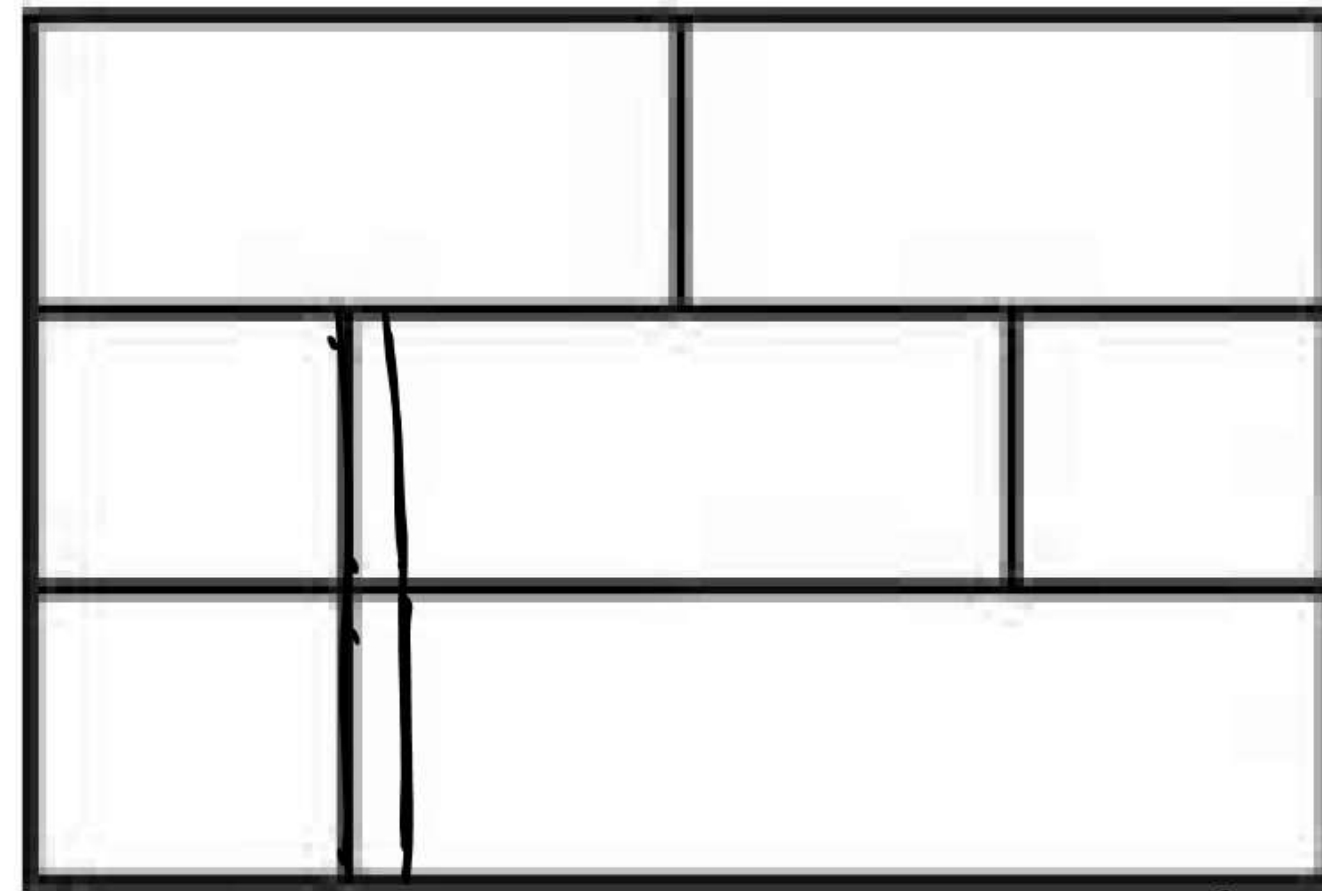
(d) 17

How many quadrilaterals are there in the given figure?

दी गई आकृति में कितने चतुर्भुज हैं?



$$1 + 2 + 3 + 2 + 2 + 3 + 2 + 2$$



(a) 18

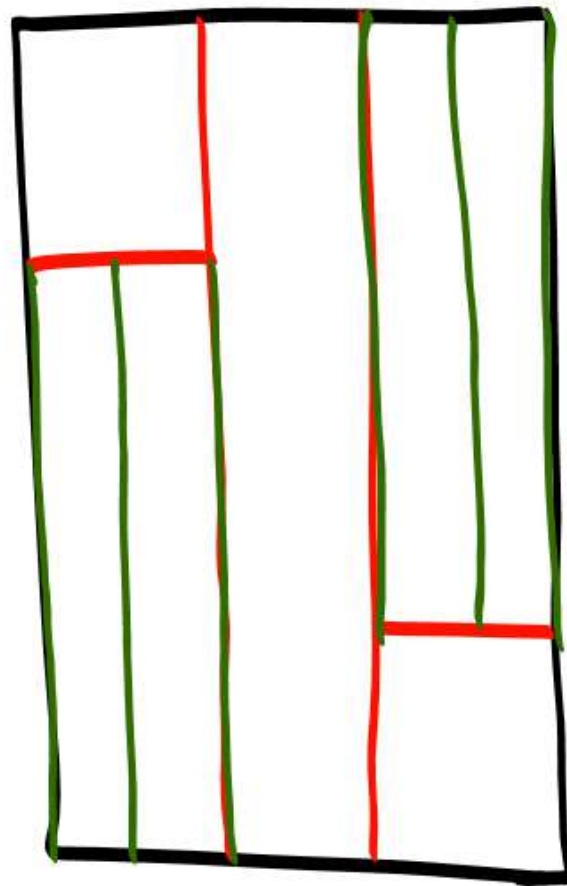
(c) 16

☒ (b) 17

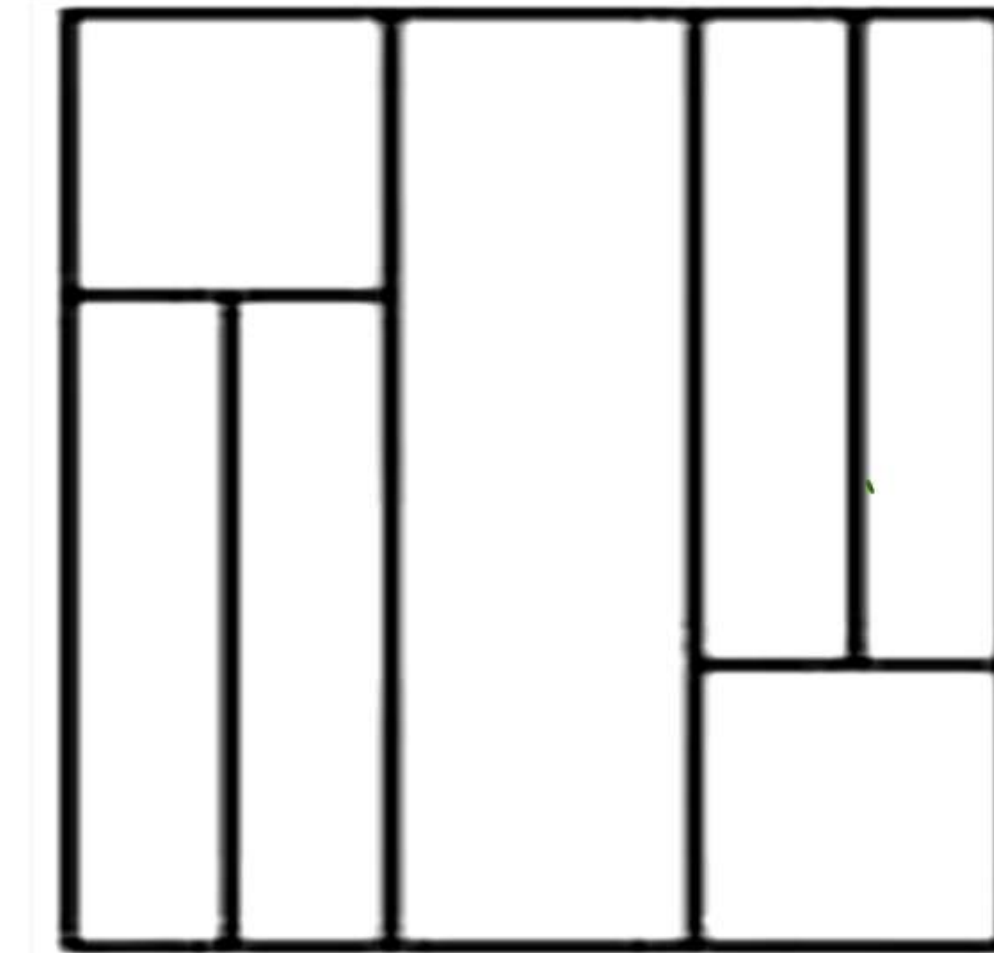
(d) 15

How many quadrilaterals are there in the given figure?

दी गई आकृति में कितने चतुर्भुज हैं?



$$1+2+3+2+2+2+2$$



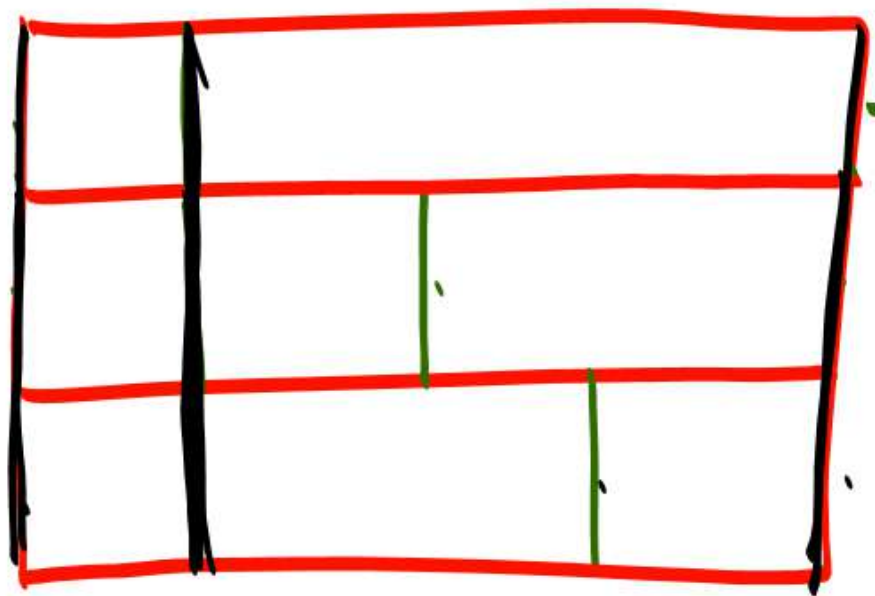
(a) 15

(c) 16

✓ (b) 14

(d) 13

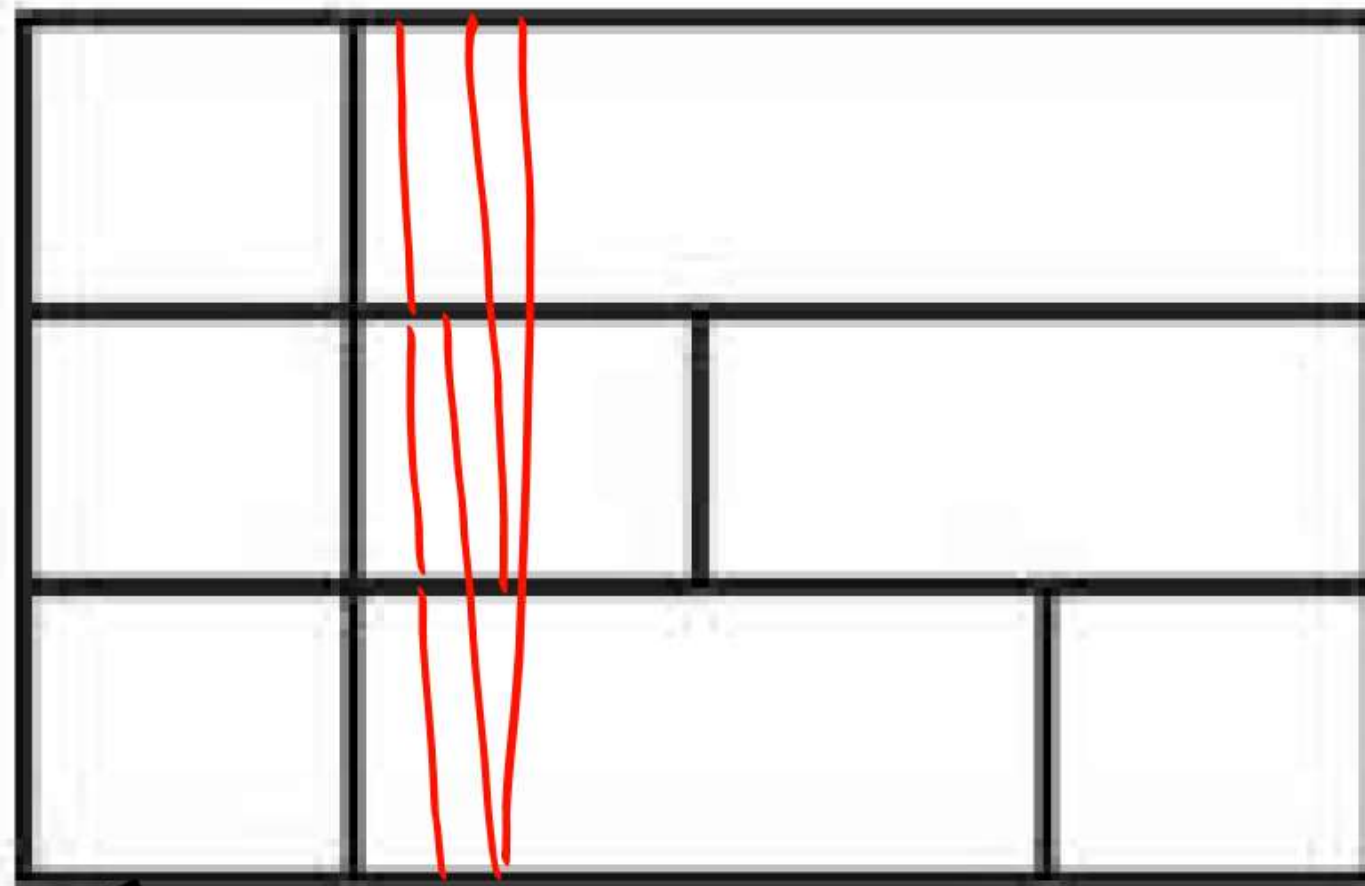
Note



$$\begin{aligned}
 & \overline{1+2+3} + \overline{2+2+2+3+2} \\
 & + \overline{3+2+2}
 \end{aligned}$$

How many quadrilaterals are there in the given figure?

दी गई आकृति में कितने चतुर्भुज हैं?

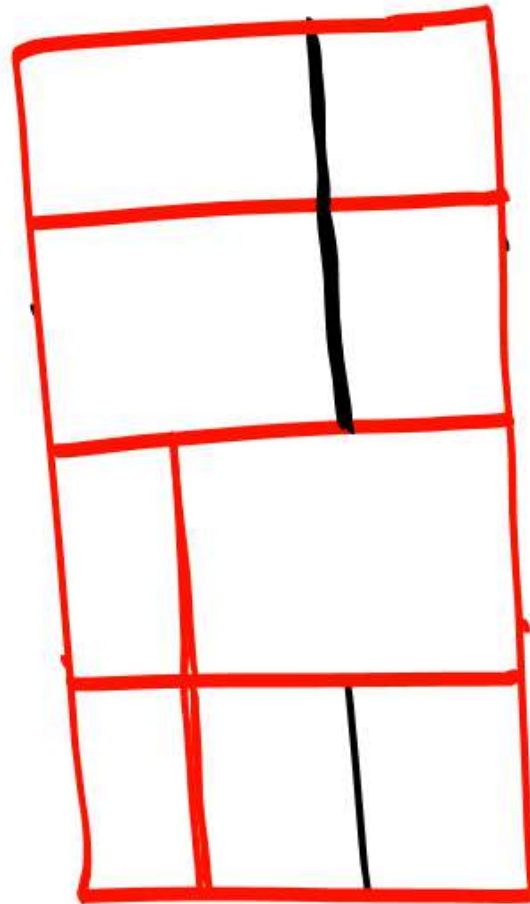


(a) 24
(c) 23

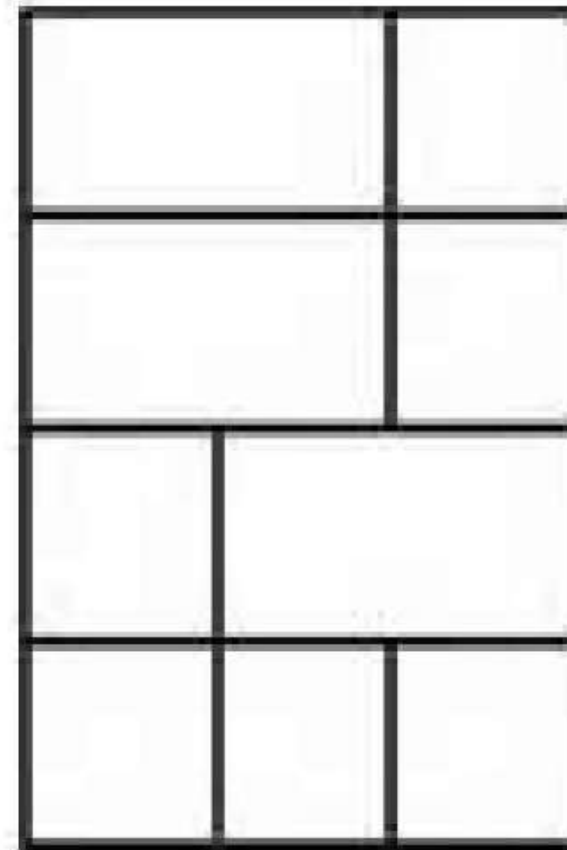
(b) 21
(d) 22

How many quadrilaterals are there in the given figure?

दी गई आकृति में कितने चतुर्भुज हैं?



$$1 + 2 + 3 + 4 + 2 + 2 + 2 + 2 + 2 + 3 + 2$$



(a) 24

(c) 22

☒ (b) 25

(d) 23